

University of Groningen

Phase space geometry and invariant manifolds underlying reaction dynamics

Krajnak, Vladimir

IMPORTANT NOTE: You are advised to consult the publisher's version (publisher's PDF) if you wish to cite from it. Please check the document version below.

Document Version

Publisher's PDF, also known as Version of record

Publication date:

2017

[Link to publication in University of Groningen/UMCG research database](#)

Citation for published version (APA):

Krajnak, V. (2017). *Phase space geometry and invariant manifolds underlying reaction dynamics*. [Thesis fully internal (DIV), University of Groningen]. Rijksuniversiteit Groningen.

Copyright

Other than for strictly personal use, it is not permitted to download or to forward/distribute the text or part of it without the consent of the author(s) and/or copyright holder(s), unless the work is under an open content license (like Creative Commons).

The publication may also be distributed here under the terms of Article 25fa of the Dutch Copyright Act, indicated by the "Taverne" license. More information can be found on the University of Groningen website: <https://www.rug.nl/library/open-access/self-archiving-pure/taverne-amendment>.

Take-down policy

If you believe that this document breaches copyright please contact us providing details, and we will remove access to the work immediately and investigate your claim.

Downloaded from the University of Groningen/UMCG research database (Pure): <http://www.rug.nl/research/portal>. For technical reasons the number of authors shown on this cover page is limited to 10 maximum.

Bibliography

- [Arn76] V. I. Arnold. *Les méthodes mathématiques de la mécanique classique*. Nauka, Moscow, Éditions Mir, 1976.
- [BGH85] J. Binney, O. E. Gerhard, and P. Hut. Structure of surfaces of section. *Mon. Not. R. Astr. Soc.*, 215(1):59–65, 1985.
- [Bir27] G. D. Birkhoff. *Dynamical Systems*. AMS, 1927.
- [Bow14] J. M. Bowman. Roaming radicals. *Mol. Phys.*, 112(19):2516–2528, 2014.
- [BS11] J. M. Bowman and B. C. Shepler. Roaming radicals. *Annu. Rev. Phys. Chem.*, 62:531–553, 2011.
- [Che86] W. J. Chesnavich. Multiple transition states in unimolecular reactions. *J. Chem. Phys.*, 84(5):2615–2619, 1986.
- [CHM75] S. Chapman, S. M. Hornstein, and W. H. Miller. Accuracy of transition state theory for the threshold of chemical reactions with activation energy. Collinear and three-dimensional $\text{H} + \text{H}_2$. *J. Am. Chem. Soc.*, 97(4):892–894, 1975.
- [Con68] C. C. Conley. Low energy transit orbits in the restricted three-body problem. *SIAM J. Appl. Math.*, 16:732–746, 1968.
- [CSB80] W. J. Chesnavich, T. Su, and M. T. Bowers. Collisions in a noncentral field: A variational and trajectory investigation of ion-dipole capture. *J. Chem. Phys.*, 72(4):2641, 1980.
- [Dav87] M. J. Davis. Phase space dynamics of bimolecular reactions and the breakdown of transition state theory. *J. Chem. Phys.*, 86(7):3978–4003, 1987.

- [EW91] B. Eckhardt and D. Wintgen. Indices in classical mechanics. *J. Phys. A*, 24(18):4335, 1991.
- [Fen71] N. Fenichel. Persistence and smoothness of invariant manifolds for flows. *Indiana Univ. Math. J.*, 21:193–226, 1971.
- [Gre68] J. M. Greene. Two-dimensional measure-preserving mappings. *Journal of Mathematical Physics*, 9(5):760–768, 1968.
- [HCB16] P. L. Huston, R. Conte, and J. M. Bowman. Roaming under the microscope: Trajectory study of formaldehyde dissociation. *J. Phys. Chem. A*, 120:5103–5114, 2016.
- [Hen82] J. Henrard. Capture into resonance: An extension of the use of adiabatic invariants. *Celestial mechanics*, 27(1):3–22, 1982.
- [Hil05] G. W. Hill. *Collected Mathematical Works of G. W. Hill, vol. 1*. Washington: Carnegie Institute, 1905.
- [Hor38] J. Horiuti. On the statistical mechanical treatment of the absolute rate of chemical reaction. *Bull. Chem. Soc. Jpn.*, 13(1):210–216, 1938.
- [HPS77] M. W. Hirsch, C. C. Pugh, and M. Shub. *Invariant Manifolds*. Lecture Notes in Mathematics. Springer-Verlag Berlin Heidelberg, 1977.
- [HSD04] M. W. Hirsch, S. Smale, and R. L. Devaney. *Differential Equations, Dynamical Systems, and an Introduction to Chaos*. Elsevier, 2004.
- [InPS11] M. Iñarra, A. I. Palacián, J. F. and Pascual, and J. P. Salas. Bifurcations of dividing surfaces in chemical reactions. *J. Chem. Phys.*, 135(1):014110, 2011.
- [JFU99] C. Jaffé, D. Farrelly, and T. Uzer. Transition state in atomic physics. *Phys. Rev. A*, 60(5):3833, 1999.
- [JRL⁺02] C. Jaffé, S. D. Ross, M. W. Lo, J. Marsden, D. Farrelly, and T. Uzer. Statistical theory of asteroid escape rates. *Phys. Rev. Lett.*, 89:011101, 2002.
- [JSG91] M. J. T. Jordan, S. C. Smith, and R. G. Gilbert. Variational transition state theory: A simple model for dissociation and recombination reactions of small species. *J. Phys. Chem.*, 95(22):8685–8694, 1991.

- [Kec67] J. C. Keck. Variational theory of reaction rates. *Adv. Chem. Phys.*, 13:85, 1967.
- [Mac90] R. S. MacKay. Flux over a saddle. *Phys. Lett. A*, 145(8,9):425–427, 1990.
- [MCE⁺85] J. D. Meiss, J. R. Cary, D. F. Escande, R. S. MacKay, I. C. Percival, and J. L. Tennyson. Dynamical theory of anomalous particle transport. *Plasma Physics and Controlled Nuclear Fusion Research 1984 Vol.3*, pages 441–448, 1985.
- [MCE⁺14a] F. A. L. Mauguière, P. Collins, G. S. Ezra, S. C. Farantos, and S. Wiggins. Multiple transition states and roaming in ion–molecule reactions: A phase space perspective. *Chem. Phys. Lett.*, 592:282–287, 2014.
- [MCE⁺14b] F. A. L. Mauguière, P. Collins, G. S. Ezra, S. C. Farantos, and S. Wiggins. Roaming dynamics in ion-molecule reactions: Phase space reaction pathways and geometrical interpretation. *J. Chem. Phys.*, 140(13):134112, 2014.
- [MCEW13] F. A. L. Mauguière, P. Collins, G. S. Ezra, and S. Wiggins. Bond breaking in a Morse chain under tension: Fragmentation patterns, higher index saddles, and bond healing. *The Journal of Chemical Physics*, 138(13):134118, 2013.
- [McG69] R. P. McGehee. Some homoclinic orbits in the restricted three-body problem. *PhD thesis*, 1969.
- [MCK⁺15] F. A. L. Mauguière, P. Collins, Z. C. Kramer, B. K. Carpenter, G. S. Ezra, S. C. Farantos, and S. Wiggins. Phase space structures explain hydrogen atom roaming in formaldehyde decomposition. *J. Phys. Chem. Lett.*, 6(20):4123–4128, 2015.
- [MCK⁺16] F. A. L. Mauguière, P. Collins, Z. C. Kramer, B. K. Carpenter, G. S. Ezra, S. C. Farantos, and S. Wiggins. Phase space barriers and dividing surfaces in the absence of critical points of the potential energy: Application to roaming in ozone. *J. Chem. Phys.*, 144(5):54107, 2016.
- [Mei15] J. D. Meiss. Thirty years of turnstiles and transport. *Chaos*, 25(9):097602, 2015.
- [Mil76] W. H. Miller. Unified statistical model for “complex $\hat{A}'\hat{A}'$ ” and “direct $\hat{A}'\hat{A}'$ ” reaction mechanisms. *J. Chem. Phys.*, 65(6):2216–2223, 1976.

- [MK71] K. Morokuma and M. Karplus. Collision dynamics and the statistical theories of chemical reactions. ii. Comparison of reaction probabilities. *The Journal of Chemical Physics*, 55(1):63–75, 1971.
- [MMP84] R. S. MacKay, J. D. Meiss, and I. C. Percival. Transport in Hamiltonian systems. *Phys. D*, 13(1-2):55–81, 1984.
- [MMW98] C. K. McCord, K. R. Meyer, and Q. Wang. The integral manifolds of the three-body problem. *Mem. Amer. Math. Soc.*, 132(628), 1998.
- [MS14] R. S. MacKay and D. C. Strub. Bifurcations of transition states: Morse bifurcations. *Nonlinearity*, 27(5):859–895, 2014.
- [MS15] R. S. MacKay and D. C. Strub. Morse bifurcations of transition states in bimolecular reactions. *Nonlinearity*, 28(12):4303, 2015.
- [OdAdLMM90] A. M. Ozorio de Almeida, N. de Leon, M. A. Mehta, and C. C. Marston. Geometry and dynamics of stable and unstable cylinders in hamiltonian systems. *Physica D*, 46(2):265–285, 1990.
- [Ott89] J. M. Ottino. *The Kinematics of Mixing: Stretching, Chaos, and Transport*. Cambridge Texts in Applied Mathematics. Cambridge Univerversity Press, 1989.
- [PCP80] P. Pollak, M. S. Child, and P. Pechukas. Classical transition state theory: A lower bound to the reaction probability. *The Journal of Chemical Physics*, 72(3):1669–1678, 1980.
- [Pec76a] P. Pechukas. On simple saddle points of a potential surface, the conservation of nuclear symmetry along paths of steepest descent, and the symmetry of transition states. *J. Chem. Phys.*, 64:1516–1521, 1976.
- [Pec76b] P. Pechukas. Statistical approximations in collision theory. In H. W. Miller, editor, *Dynamics of Molecular Collisions Part B*, pages 269–322. Plenum Press, 1976.
- [Pec81] P. Pechukas. Transition state theory. *Ann. Rev. Phys. Chem.*, 32(1):159–177, 1981.
- [PK64] R. N. Porter and M. Karplus. Potential energy surface for H₃. *J. Chem. Phys.*, 40(4):1105–1115, 1964.
- [PM73] P. Pechukas and F. J. McLafferty. On transition-state theory and the classical mechanics of collinear collisions. *J. Chem. Phys.*, 58:1622–1625, 1973.

- [PP78] E. Pollak and P. Pechukas. Transition states, trapped trajectories, and classical bound states embedded in the continuum. *J. Chem. Phys.*, 69(3):1218–1226, 1978.
- [PP79a] P. Pechukas and E. Pollak. Classical transition state theory is exact if the transition state is unique. *J. Chem. Phys.*, 71(5):2062–2068, 1979.
- [PP79b] E. Pollak and P. Pechukas. Unified statistical model for “complex” and “direct” reaction mechanisms: A test on the collinear H+H₂ exchange reaction. *J. Chem. Phys.*, 70(1):325–333, 1979.
- [QH84] W. Quapp and D. Heidrich. Analysis of the concept of minimum energy path on the potential energy surface of chemically reacting systems. *Theoret. Chim. Acta (Berl.)*, 66(3):245–260, 1984.
- [RKW90] V. Rom-Kedar and S. Wiggins. Transport in two-dimensional maps. *Arch. Ration. Mech. Anal.*, 109(3):239–298, 1990.
- [Rui75] O. R. Ruiz. Existence of brake-orbits in Finsler mechanical systems. *PhD thesis*, 1975.
- [SA97] K. R. Sreenivasan and R. A. Antonia. The phenomenology of small-scale turbulence. *Annu. Rev. Fluid Mech.*, 29(1):435–472, 1997.
- [Sei45] H. Seifert. Periodische Bewegungen mechanischer Systeme. *Math. Z.*, (41):197–216, 1945.
- [SK78] D. I. Sverdlik and G. W. Koeppel. An energy limit of transition state theory. *Chem. Phys. Lett.*, 59(3):449–453, 1978.
- [Sre91] K. R. Sreenivasan. On local isotropy of passive scalars in turbulent shear flows. *Proc. R. Soc. London. Ser. A*, 434(1890):165–182, 1991.
- [TG84] G. D. Truhlar and B. C. Garrett. Variational transition state theory. *Ann. Rev. Phys. Chem.*, 35:159–189, 1984.
- [TKK⁺05] M. Toda, T. Komatsuzaki, T. Konishi, R. S. Berry, and S. A. Rice, editors. *Geometric Structures of Phase Space in Multidimensional Chaos*. John Wiley & Sons, Inc., 2005.
- [TLL⁺04] D. Townsend, A. Lahankar, S. K. Lee, S. D. Chambreau, A. G. Suits, X. Zhang, J. Rheinecker, L. B. Harding, and J. M. Bowman. The roaming atom: Straying from the reaction path in formaldehyde decomposition. *Science*, 306(5699):1158–1161, 2004.

- [UJP⁺02] T. Uzer, C. Jaffé, J. Palacián, P. Yanguas, and S. Wiggins. The geometry of reaction dynamics. *Nonlinearity*, 15:957–992, 2002.
- [vZFM93] R. D. van Zee, M. F. Foltz, and C. B. Moore. Evidence for a second molecular channel in the fragmentation of formaldehyde. *J. Chem. Phys.*, 99(3):1664–1673, 1993.
- [WBW04a] H. Waalkens, A. Burbanks, and S. Wiggins. A computational procedure to detect a new type of high-dimensional chaotic saddle and its application to the 3D Hill’s problem. *J. Phys. A*, 37:L257–L265, 2004.
- [WBW04b] H. Waalkens, A. Burbanks, and S. Wiggins. Phase space conduits for reaction in multidimensional systems: HCN isomerization in three dimensions. *J. Chem. Phys.*, 121(13):6207–6225, 2004.
- [WBW05a] H. Waalkens, A. Burbanks, and S. Wiggins. Efficient procedure to compute the microcanonical volume of initial conditions that lead to escape trajectories from a multidimensional potential well. *Phys. Rev. Lett.*, 95:084301, 2005.
- [WBW05b] H. Waalkens, A. Burbanks, and S. Wiggins. A formula to compute the microcanonical volume of reactive initial conditions in transition state theory. *J. Phys. A*, 38:L759–L768, 2005.
- [Wig37] E. Wigner. Calculation of the rate of elementary association reactions. *J. Chem. Phys.*, 5:720–725, 1937.
- [Wig38] E. Wigner. The transition state method. *Trans. Faraday Soc.*, 34:29–41, 1938.
- [Wig03] S. Wiggins. *Introduction to Applied Nonlinear Dynamical Systems and Chaos*. Springer, New York, 2003.
- [Wil36] J. Williamson. On the algebraic problem concerning the normal forms of linear dynamical systems. *American Journal of Mathematics*, 58(1):141–163, 1936.
- [WSW08] H. Waalkens, R. Schubert, and S. Wiggins. Wigner’s dynamical transition state theory in phase space: classical and quantum. *Nonlinearity*, 21:R1–R118, 2008.
- [WW04] H. Waalkens and S. Wiggins. Direct construction of a dividing surface of minimal flux for multi-degree-of-freedom systems that cannot be recrossed. *J. Phys. A*, 37:L435, 2004.

- [WW10] H. Waalkens and S. Wiggins. Geometric models of the phase space structures governing reaction dynamics. *Reg. Chaot. Dyn.*, 15:1–39, 2010.
- [WWJU01] S. Wiggins, L. Wiesenfeld, C. Jaffé, and T. Uzer. Impenetrable barriers in phase-space. *Phys. Rev. Lett.*, 86:5478–5481, 2001.